# Deformation Analysis of Ground Foundation — Usage and theory of DACSAR

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### **DACSAR stands for**

Deformation Analysis Considering Stress Anisotropy and Reorientation

**DACSAR** Soil and water coupled Elasto-viscoplastic F.E. code

- open to the public -



Bulletin Laboratoires des Ponts et Chaussees, 232, pp.45-60, 2001 MOMIS: A database for the numerical modeling of embankments on soft soils and the comparison between computational

The figure shows the result of investigation by LCPC. DACSAR is one of the most popular program to predict the soil behavior.



ROSALIE-LCPC have been combined in this figure).

### DACSARs:

- DACSAR (DACSAR-original)
  - Open to the public
- DACSAR-MC (DACSAR-updated)
  - \* EC/LC model is incorporated;
  - \* Subloading surface;
  - \* Macro element is incorporated;
  - Open to the public
- DACSAR-3D (3-Dimensional version of DACSAR) Not open to the public
- DACSAR-F (finite deformation version of DACSAR)
  - Soil/water coupled elasto-plastic FE based on incremental finite deformation theory Not open to the public
- DACSAR-U
  - Unsaturated soil/water coupled elasto-plastic FE Not open to the public
- > DACSAR-D
  - Dynamic soil/water coupled elasto-plastic FE Not open to the public

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# **1-DESCRIPTION of DACSAR**

- Introduction
- Origination of report
- > Program overview





### > Preface

- > 1-Description of DACSAR
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# 2-Details of theories used in DACSAR

- 1. Constitutive models employed in DACSAR
- 2. Singular point on the yielding surface (SO)
- 3. Yielding Judgment
- 4. Metastability (SO-EP)
- 5. Functions
- 6. Macro element proposed by Sekiguchi et al.
- 7. Bar, Beam, Joint, Shell element etc.

# 1.Constitutive models employed in DACSAR

**1.1 Theoretical explanation** 

**1.2 Demonstration** 



### **1.1 Theoretical explanation**

MT	Element type	
0	Elasto-(visco)plastic plane element	
1	Linearly elastic plain element	
2	Linearly elastic Beam element	
3	Linearly elastic Bar element	
4	Elastic perfectly plastic Joint element	
5	Linearly plastic Shell element	Constitutive
6	Drucker-Prager plane element	discussed
7	Hyperbolic plane element	here
8	Modified Cam-Clay model	
9	EC model element	
10	LC model element	

### 1.1 Theoretical explanation

Constitutive m	nodels used in DACSAR
MT	Model type
MT=0	Sekiguchi-Ohta model, includs
	(1) SO-EP model
	(2) SO-EVP model;
	(3) SO-EP with subloading surface model(SOSS model)
MT=1	Linear elastic materials
MT=6	Drucker-Prager model
MT=7	Hyperbolic materials
MT=8	Modified Cam-Clay model
MT=9	EC model (Exponential contractancy model), includs
	(1) EC-EP model
	(2) EC-EVP model
	(3) EC-EP with subloading surface model(SOSS model)
MT=10	LC model (Logarithmic contractancy model), includs
	(1) LC-EP model
	(2) LC-EVP model
	(3) LC-EP with subloading surface model(SOSS model)

### MT=0, Sekiguchi-Ohta model



(a) Yield surface of SO-E(V)P model

(b) Sketch of subloading surface

Fig1.1 Yield surface of SO model

### MT=6, Drucker-Prager model MT=8, Modified Cam-Clay model



Fig1.2 Yield surface of DP model in principal stress space Fig1.3 Yield surface of Modified Cam-Clay model

### MT=9, EC model (Exponential contractancy model) MT=10, LC model (Logarithmic contractancy model)



### Case 0 for 1D consolidation for OCR=1

1D consolidation	Linear model	SO model	DP model	EC model	LC model
for OCR=1			case 0		

### Value of parameters

Lame's	Permeability			
$\widetilde{\lambda}(kg/cm^2)$	$\widetilde{\mu}(kg/cm^2)$	$k(cm/\min)$		
13.661	6.805	6.0*10 <sup>-6</sup>		



Fig1.6 Boundary condition for Case 0



Fig1.7(a) Relationship between degree of consolidation and time factor



**Fig1.7**(b) Consolidation Isochrone for Case 0 by using linear elastic model

Case  $(1-1) \sim (3-19)$  for the application of different constitutive models with different value of OCR and different drainage condition

OCR	Drainage condition	SO- model		EC-model		LC-model				
		EP	EVP	SS	EP	EVP	SS	EP	EVP	SS
1	Undrained	(1-1)	(1-2)	(1-3)	(1-4)	(1-5)	(1-6)	(1-7)	(1-8)	(1-9)
	Fully draind	(1-11)	(1-12)	(1-13)	(1-14)	(1-15)	(1-16)	(1-17)	(1-18)	(1-19)
2	Undrained	(2-1)	(2-2)	(2-3)	(2-4)	(2-5)	(2-6)	(2-7)	(2-8)	(2-9)
	Fully draind	(2-11)	(2-12)	(2-13)	(2-14)	(2-15)	(2-16)	(2-17)	(2-18)	(2-19)
20	Undrained	(3-1)	(3-2)	(3-3)	(3-4)	(3-5)	(3-6)	(3-7)	(3-8)	(3-9)
	Fully draind	(3-11)	(3-12)	(3-13)	(3-14)	(3-15)	(3-16)	(3-17)	(3-18)	(3-19)

Three types of tests including plane strain shear, axisymmetric shear and direct shear



**Fig1.8** Three types of tests

### Effect of corresponding parameter to some model is considered

	Elasto-plastic	Elasto-viscoplastic	Subloading surface
SO model			
EC model	$n_E = 1.0$ (SO model) $n_E = 1.5$ $n_E = 2.0$	$\dot{\varepsilon}_z(\dot{\varepsilon}_a) = 0.1\%/\min$	m = 1 $m = 10$
LC model	$n_L = 1.5$ $n_L = 2.0$ $n_L = 2.5$	$\dot{\varepsilon}_z(\dot{\varepsilon}_a) = 0.01\%/\min$	<i>m</i> = 100



#### Input parameters

D	0.076	$\sigma'_{v0}(\text{kg/cm}^2)$	1.0
Λ	0.549	$\sigma'_{vi}$ (kg/cm <sup>2</sup> )	1.0
M	0.961	$\dot{v}_0(1/\text{min})$	0.001%
$\nu'$	0.394	λ	0.245
$K_0$	0.65	$K_i$	0.65
α	0.00667	$e_0$	0. 84



### Case1-1 SO-EP model for undrained condition with OCR=1

(Same with Case1-3 SO-SS model)



**Fig1.10** Stress-strain relation and effective stress path

### Case1-2 SO-EVP model for undrained condition with OCR=1



 $\dot{\varepsilon}_z(\dot{\varepsilon}_a) = 0.1\%/\text{min}$ 

### **Fig1.11 Stress-strain relation and effective stress path**

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#### Case1-4 EC-EP model for undrained condition with OCR=1

(Same with Case1-6 EC-SS model)



 $n_{E} = 1.5$ 

**Fig1.12** Stress-strain relation and effective stress path

#### Case1-5 EC-EVP model for undrained condition with OCR=1



**Fig1.13 Stress-strain relation and effective stress path** 

### Case1-7 LC-EP model for undrained condition with OCR=1

(Same with Case1-9 LC-SS model)



 $n_{L} = 2$ 

**Fig1.14 Stress-strain relation and effective stress path** 

#### Case1-8 LC-EVP model for undrained condition with OCR=1



**Fig1.15 Stress-strain relation and effective stress path** 

#### **Case2-1 SO-EP model for undrained condition with OCR=2**



**Fig1.16 Stress-strain relation and effective stress path** 

### **Case3-1 SO-EP model for undrained condition with OCR=20**



**Fig1.17** Stress-strain relation and effective stress path

#### **Case3-3 SO-SS model for undrained condition with OCR=20**



**Fig1.18 Stress-strain relation and effective stress path** 

#### **Case3-3 SO-SS model for undrained condition with OCR=20**



**Fig1.19** Stress-strain relation and effective stress path

#### **Case3-3 SO-SS model for undrained condition with OCR=20**



**Fig1.20** Stress-strain relation and effective stress path

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# 2. Singular point on the yielding surface (Takeyama,2007, Doctoral dissertation)

**2.1 Explanation of theoretical treatment** 

**2.2 Demonstration** 


## 2.1 Theoretical explanation



Fig 2.1 Singular point on the yield surface of SO model

### 2.1 Theoretical explanation

# Governing function for the singular point

Koiter's associated flow rule:  $\dot{\varepsilon}^{\rm p} = \dot{\gamma}_1 \partial_{\sigma'} f_1 + \dot{\gamma}_2 \partial_{\sigma'} f_2$ Consistency condition:  $\dot{f}_1 = 0, \dot{f}_2 = 0$  $f_1(\sigma', \varepsilon_v^p) = MD \ln \frac{p'}{n'_{\nu}} + D\sqrt{\frac{3}{2}} \frac{\left(\overline{\mathbf{s}} : \overline{\mathbf{n}}_v\right)}{n'_{\nu}} - \varepsilon_v^p = 0$ Yield function:  $f_2(\sigma',\varepsilon_v^{\rm p}) = MD\ln\frac{p'}{n'} - D\sqrt{\frac{3}{2}\frac{\left(\overline{s}:\overline{n}_v\right)}{n'}} - \varepsilon_v^{\rm p} = 0$ Plastic proportional coefficient:  $\begin{cases} \dot{\gamma}_{1} \\ \dot{\gamma}_{2} \end{cases} = \frac{1}{\det X} \begin{bmatrix} X_{22} & -X_{12} \\ -X_{21} & X_{11} \end{bmatrix} \begin{bmatrix} L_{1} \\ L_{2} \end{bmatrix}$ where, det  $X = X_{11}X_{22} - X_{12}X_{21}$  $X_{11} = \frac{D^2}{{n'}^2} \left( \beta_1^2 K + 3G + \frac{p'}{D} \beta_1 \right), \quad X_{12} = \frac{D^2}{{n'}^2} \left( \beta_1 \beta_2 K - 3G + \frac{p'}{D} \beta_2 \right)$  $X_{21} = \frac{D^2}{{p'}^2} \left( \beta_1 \beta_2 K - 3G + \frac{p'}{D} \beta_1 \right), \quad X_{22} = \frac{D^2}{{p'}^2} \left( \beta_2^2 K + 3G + \frac{p'}{D} \beta_2 \right)$  $\beta_{1} = \mathbf{M} \cdot \sqrt{\frac{3}{2}} (\eta_{0} : \overline{\mathbf{n}}_{\nu}), \beta_{2} = \mathbf{M} \cdot \sqrt{\frac{3}{2}} (\eta_{0} : \overline{\mathbf{n}}_{\nu}), \overline{\mathbf{n}}_{\nu} = \frac{(1 - \Lambda) K \dot{\varepsilon}_{\nu} \eta_{0} - 2G \dot{\varepsilon}_{d}}{\|(1 - \Lambda) K \dot{\varepsilon}_{\nu} \eta_{0} - 2G \dot{\varepsilon}_{d}\|}$ 

## **2.2 Demonstration**



(a) Effective stress path

(b) *e*-ln*p* ' relation

Fig 2.3 Simulation result of effective stress path and *e*-ln*p*' relation near to singular point on the yielding surface of SO model before coping the singular point

## **2.2 Demonstration**



(a) Effective stress path

(b) *e*-ln*p* ' relation

Fig 2.4 Simulation result of effective stress path and e-Inp' relation near to singular point on the yielding surface of SO model after coping the singular point

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# **3. Yielding Judgment** (Takeyama,2007, Doctoral dissertation)

- 3.1 Improved Yielding judgment criterion for SO-EVP, EC-EVP, LC-EVP model
- 3.2 Corrected Akai & Tamura's method for spatially discretization of pore water dissipation
- 3.3 1D consolidation (coupled) for Linearly elastic body by using two types of mesh generations



# Improved judgment criterion

(1) For elastic state

$$\begin{cases} g(\sigma',h) = f(\sigma') - h < 0: & \text{elastic} \\ g(\sigma',h) = f(\sigma') - h \ge 0: & \text{elasto - visco - plastic} \end{cases}$$

(2) For elasto-visco-plastic state

 $\begin{cases} \gamma < 0 : & \text{elastic} \\ \gamma \ge 0 : & \text{elasto - visco - plastic} \end{cases}$ 



For SO-EVP 
$$f = MD \ln \frac{p'}{p'_0} + D \cdot \eta *$$
,

For EC-EVP 
$$f = MD \ln \frac{p'}{p'_0} + \frac{MD}{n_E} \cdot \left(\frac{\eta *}{M}\right)^{n_E}$$

For LC-EVP 
$$f = MD \ln \frac{p'}{p'_0} + \frac{2MD}{n_L} \cdot \ln \left[1 + \left(\frac{\eta *}{M}\right)^{n_L}\right]$$

$$g(\sigma',h) = f(\sigma') - h = 0$$

$$h(\varepsilon_{v}^{p},t) = \alpha \cdot \ln\left\{\frac{\alpha}{\dot{v}_{0}t}\left[\exp\left(\frac{\varepsilon_{v}^{vp}}{\alpha}\right) - 1\right]\right\}$$

$$\gamma = -\frac{\frac{\partial F}{\partial \sigma'} : C^{e} : \dot{\varepsilon} + \frac{\partial F}{\partial t}}{\frac{\partial F}{\partial \sigma'} : C^{e} : \frac{\partial F}{\partial \sigma'} - \frac{\partial F}{\partial \varepsilon_{v}^{vp}} \frac{\partial F}{\partial p'}}, \text{ is plastic coefficient, } \dot{\varepsilon}_{v}^{vp} = \gamma \frac{\partial F}{\partial p'}$$

# Yielding judgment criterion for SO model at the singular point



$$\begin{cases} \dot{\gamma}_{1} \\ \dot{\gamma}_{2} \end{cases} = \frac{1}{\det X} \begin{bmatrix} X_{22} & -X_{12} \\ -X_{21} & X_{11} \end{bmatrix} \begin{bmatrix} L_{1} \\ L_{2} \end{bmatrix}$$
  
where, det  $X = X_{11}X_{22} - X_{12}X_{21}$   
 $X_{11} = \frac{D^{2}}{p'^{2}} \Big( \beta_{1}^{2}K + 3G + \frac{p'}{D}\beta_{1} \Big), \quad X_{12} = \frac{D^{2}}{p'^{2}} \Big( \beta_{1}\beta_{2}K - 3G + \frac{p'}{D}\beta_{2} \Big)$   
 $X_{21} = \frac{D^{2}}{p'^{2}} \Big( \beta_{1}\beta_{2}K - 3G + \frac{p'}{D}\beta_{1} \Big), \quad X_{22} = \frac{D^{2}}{p'^{2}} \Big( \beta_{2}^{2}K + 3G + \frac{p'}{D}\beta_{2} \Big)$   
 $\beta_{1} = M - \sqrt{\frac{3}{2}} (\eta_{0} : \overline{\eta}_{v}), \beta_{2} = M - \sqrt{\frac{3}{2}} (\eta_{0} : \overline{\eta}_{v}), \overline{\eta}_{v} = \frac{(1 - \Lambda)K\dot{\varepsilon}_{v}\eta_{0} - 2G\dot{\varepsilon}_{d}}{\|(1 - \Lambda)K\dot{\varepsilon}_{v}\eta_{0} - 2G\dot{\varepsilon}_{d}\|}$ 



## 3.2 Corrected Akai & Tamura's method



Fig3.3 Method for Spatially discretization of pore water dissipation (consolidation) be corrected

## 3.3 1D consolidation by using two types of mesh



Fig3.4 Simulation of 1-D consolidation by using two types of mesh

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# **4. Metastability (SO-EP)** (Takeyama,2007, Doctoral dissertation)

**4.1 Theoretical explanation** 

4.2 Demonstration



**4.1 Theoretical explanation** 

For the isotropic consolidated clay, the infinitesimal increment of stress ratio can induce a rapid plastic shear deformation, which is called Metastability characteristic (Roscoe et.al. 1963), this stress state can be called Metastable state.



**Fig4.1 Metastable area** 

## **4.2 Demontration**



Fig4.2 Simulation results of effective stress path according to given strain path for the metastable area of SO model after coping the singular point



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# 5. Functions

In DACSAR program, the numerical solution of initial boundary-value problem relies on the finite element method (FEM) based on spatial and time discretization. For the numerical integration procedures, the integration of constitutive equation over a time step to calculate the stress and strain changes corresponding to the change of the displacement is accomplished by using the algorithm to solve the systems of linear equations.

Systems of linear equations on the relation between nodal force and nodal dispalacement  $\Delta F = K \cdot \delta d$ 

where,  $K = \sum_{e} \int_{\Omega^{e}} B_{e}^{T} C^{ep} B_{e} d\Omega^{e}$ , is total stiffness matrix,

 $B_{e} = LN$ , is strain matrix, L is differential operator for plain problem,

N is shape function

# **5. Functions**

The integration technique adopted can be classified into explicit method: Gaussian method implicit method: Biconjugate gradient stabilized method and

# 5.1 Simple explicit method

# 5.2 Implicit (iterative) calculation method





## **Fig5.1 Calculation process of Gaussian method**



## **5.2 Implicit (iterative) calculation method**

## Implicit (iterative) calculation method (BiCGSTAB)

Algorithm procedure

```
Allocate temporary vectors p, \hat{p}, s, \hat{s}, t, v, \tilde{r}
Allocate temporary reals r_1, r_2, \alpha, \beta, \omega
r := \Delta F - K \cdot \delta d
\widetilde{r} = r
For i:=1 step 1 until max itr do
                r_1 = \widetilde{r} \cdot r
                If i = 1 then p := r else
                \beta = (r_1 / r_2) * (\alpha / \omega)
                 p = r + \beta * (p - \omega * v)
                End if
                Solve (M \cdot \hat{p} = p)
                v = K \hat{p}
                \alpha = r_1 / (\tilde{r} \cdot v)
                s = r - \alpha \cdot v
                Solve (M \cdot \hat{s} = s)
                t = K \cdot \hat{s}
                \omega = (t \cdot s)/(t \cdot t)
                 x = x + \alpha \cdot \hat{p} + \omega \cdot \hat{s}
                 r = s - \omega * t
                 r_2 = r_1
End (i-loop)
Deal locate all temp memory
Return TRUE
```

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# 6. Macro element proposed by Sekiguchi, Shibata,Mimura,Sumikura(1988)

6.1 Explanation of the macro element

6.2 Explanation of input parameters for the macro element

6.3 Demonstration

- Macro element is a big physical domain which includes foundation area and vertical drain in this area.
- Acro element method is used to predict the postconstruction stress changing and deformation, especially for the plane strain problem of vertical drain casting by using the construction method such as SCP / SD/CVC
- The constitutive model of SO, linear elastic, modified cam-clay, EC and LC can be used.





- excess pore water of a centered macro element and those of the adjoining four elements
- Fig6.1 Sketch showing the freedom of Fig6.2 Sketch illustrating the distribution of excess pore water pressures around equally spaced vertical drains

## **6.1 Explanation of the macro element**



Fig6.3 Sketch illustrating the proposed way of considering water flow across the boundary between the treated and untreated regions

6.2 Explanation of input parameters for the macro element

- ✓ Model parameters
- ✓ Radius of drain
- ✓ Effective collector radius
- ✓ Boundary condition



### Material parameters for macro element

$\widetilde{\lambda}$ (kN/m <sup>2</sup> )	$\widetilde{\mu}$ (kN/m <sup>2</sup> )	$\sigma'_{\scriptscriptstyle vi}$ (kPa)	$K_i$	k (m/day)
1.338	667	9.8	0.65	8.64*10 <sup>-5</sup>

#### Three kinds of cases

Case	$S_x(=S_y)(\mathbf{m})$	$S_{z}(\mathbf{m})$	<i>a</i> (m)	<i>b</i> (m)
1	2.0	1.0	0.2	1.12838
2	1.0	1.0	0.1	0.56419
3	1.0	2.0	0.1	0.56419



# 6.3 Demonstration



Fig6.5 Relation between degree of consolidation and time factor for macro element



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# 7. Bar, Beam, shell element etc.

MT	Element type	Application element is used to represent	
		1. Flexural members in a building frame	
2 1	Linearly elastic Beam element	2. Columns in a building frame	
		3. Sheet pile walls	
3	Linearly elastic Bar element	1. Reinforcement in reinforced earth structures	
		2. Tie backs for anchor walls	
		3. Springs	
		4. Structural Braces/Struts	
4	Elastic perfectly plastic Joint element	1. Interface between soil and rock	
		2. Interface between fill and concrete retaining wall	
		3. Interface between soil and reinforcement in	
		reinforced earth structures	
		4. Rock joints/fractures	
5	Linearly plastic Shell element	Supporting structure in the ground	
7	Hyperbolic plane element	1. Saturated soil inducing fills and foundation	
		2. Mass concrete structure	
		3. Rock	

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# **3-Practical use**



# Fig.3-1 Embankment as cycle way in north of Takeo I.C



**3-Practical use** 



Fig.3-2 Sketch for one typical part of the embankment with its foundation and the boundary conditions

#### **3-Practical use**



**Fig.3-3 Monitored and Simulation results** 

# **THANKS FOR**

# **YOUR ATTENTION**

